

# ON GLOBAL HYPOELLIPTICITY OF $\bar{\partial}_b$ ON COMPACT CR MANIFOLDS

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ABSTRACT. In this work, we consider a family of compact CR manifolds, of the form  $\Omega = M \times \mathbb{T}^d$ , where  $M$  is a compact Kähler manifold. The structure depends naturally on  $d$  forms  $\omega_j$  on  $M$ , of type  $(0, 1)$  and  $\bar{\partial}$ -closed. On the Levi-flat case, we study the problem of global hypoellipticity of the associated differential operator  $\bar{\partial}_b$ . We are able to characterize this property in terms of global hypoellipticity of a real operator naturally associated to  $\bar{\partial}_b$ . Time permitting, we shall also discuss questions of solvability and cohomology for these (and related) models. This work is part of the author's PhD thesis, supervised by Paulo Cordaro.

## REFERENCES

- [1] P. D. Cordaro and V. Novelli. A comparison principle between certain Levi-flat compact CR manifolds and systems of real vector fields. *Disponível em arXiv:2311.00607*, 2023.
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